

Research Purposal For Graph theory

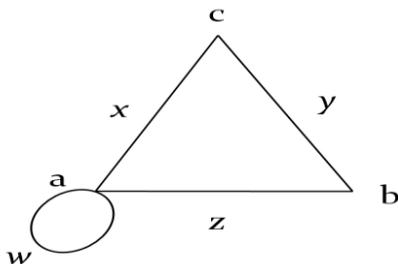
In mathematics, graph theory is the study of graphs, which are mathematical structures, used to model pair wise relations between objects. A graph in this context is made up of vertices, nodes, or points which are connected by edges, arcs, or lines.

Definitions

There is large number of definitions in graph theory. The following are some of the more basic ways of defining graphs and related mathematical structure.

Graph

a graph is an ordered pair $G = (V, E)$ consisting of a non-empty set $V = \{v_1, v_2, v_3, \dots\}$ of vertices or nodes or points together with a set $E = \{e_1, e_2, e_3, \dots\}$ of edges or arcs or lines, which are 2-element subsets of V

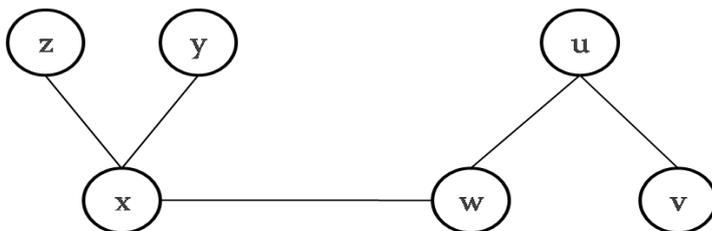


Here vertices are a, b, c and $a, b, c \in V$
And edges are w, x, y, z and $w, x, y, z \in E$

The set $V(G)$ is called the **vertex set** of G and $E(G)$ is called the **edge set**. Usually the **Graph** is denoted by $G = (V, E)$ for $u, v \in V$ set and $\{u, v\}$ an edge of G . Since $\{u, v\}$ is 2-elements set, we may write $\{v, u\}$.

If $e = uv$ is an edge of G , then we say that u and v are **adjacent** in G and e joins u and v .

For example: A graph G is denoted by the sets $V(G) = \{u, v, w, x, z\}$ and $E(G) = \{uv, uw, wx, xy, xz\}$. Now we have the following graph by considering these sets.



Types of Graphs Methodology

1. Null Graph: A graph which contains only **isolated node**, is called a null graph

i.e., the set of edges in the graph is empty.

Null graph is denoted on n vertices by N_n

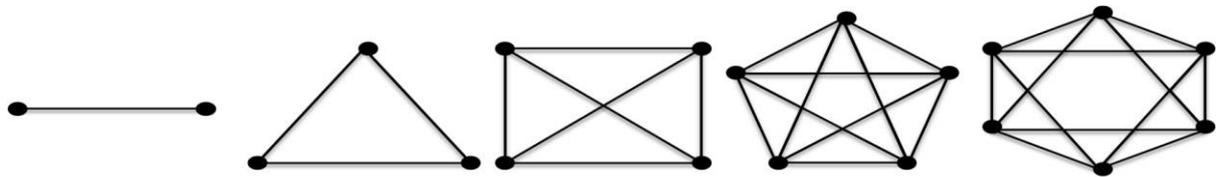
N_4 is shown in the figure 8.

2. Complete Graph: A simple graph G is said to be **complete** if every vertex in G is connected with every other vertex.

i.e., If G contains exactly one edge between each pair of distinct vertices.

A complete graph is usually denoted by K_n . It should be noted that K_n has exactly $\frac{n(n-1)}{2}$ edges.

The graph K_n for $n= 1, 2, 3, 4, 5, 6$ are shown in Fig 9.

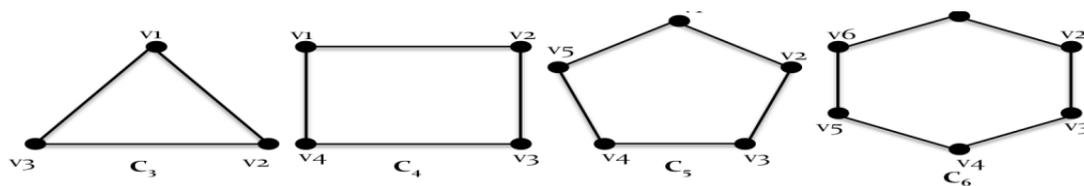


3. Regular Graph: A graph, in which all the vertices are of **Equal degree**, is called a **Regular Graph**.

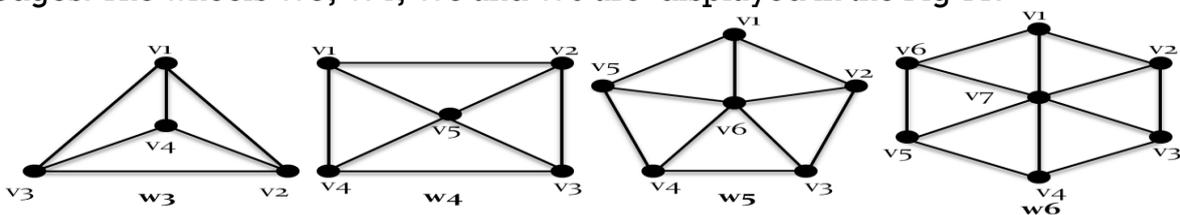
If the degree of each vertex is r , then the graph is called a regular graph of degree r .

4. Cycles: The cycle C_n , consist of n vertices v_1, v_2, \dots, v_n and edges $[v_1, v_2], [v_2, v_3], [v_3, v_4], \dots, [v_{n-1}, v_n]$.

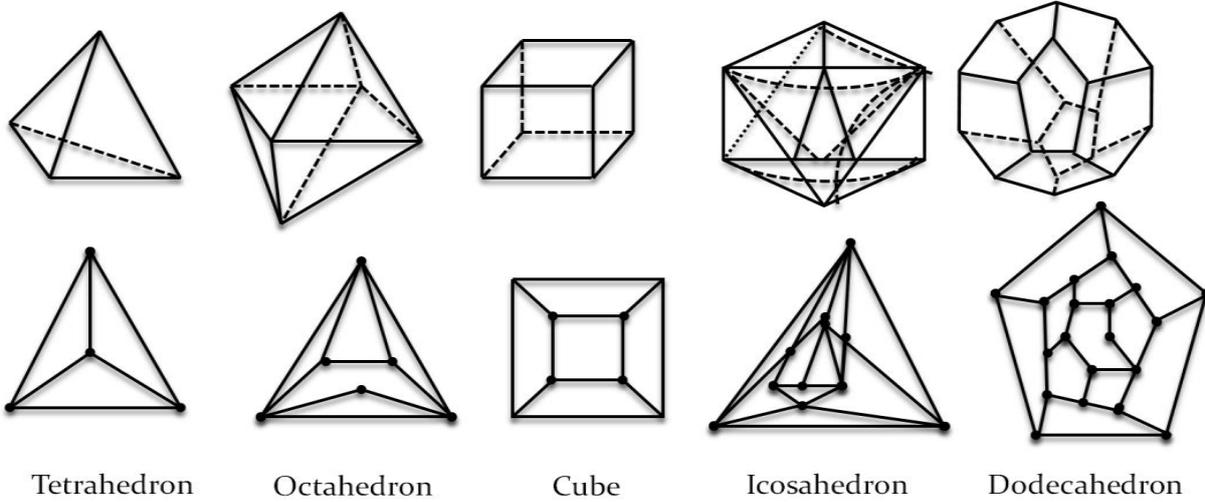
The cycles C_3, C_4, C_5 and C_6 are shown in Fig 10.



5. Wheels: The wheel W_n is obtained when an additional vertex to the cycle C_n , for $n \geq 3$, and connect this new vertex to each of the n vertices in C_n , by new edges. The wheels W_3, W_4, W_5 and W_6 are displayed in the Fig 11.



6.Platonic Graph: the graph formed by edges and vertices of five regular(platonic) solids-The tetrahedron, octahedron, cube, dodecahedron and icosahedrons.



ELEMENTS OF GRAP THEORY

TERMINOLOGY

***Loop:** an edge of the graph that joins a node to itself is called **loop** or **self-loop** i.e., a loop is an edge (v_i, v_j) where $v_i = v_j$.

***Degree of vertex:** The number of edges incident on a vertex v_j with self-loops is called the **degree of a vertex v_j** and denoted by **$\deg G(v_j)$** or **$\deg v_j$** or **$d(v_j)$** .

***Path:** An open walk in which no vertex appears more than once is called **path**. The number of edges in the path is called **length of a path**.

***Component:** disconnected graph consists of two or more connected graphs. Each of these connected subgraph is called a component.

